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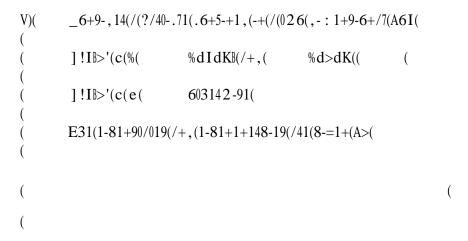
/'(O99; : -+8(03/0(031(1+148>(a \ b(-9(9 : /7714(03/+(1-0314(=/7;1(65(] !I'B(./7.;7/01(/+(1I?4199-6+(564(031(41571.01,(2/=1)(

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$$\label{eq:constraint} \begin{split} &\wedge ((j \ 6 \ ; \ (\ : \ / > (\ ; 91(031(91 \ : \ . \ . \ / 99- \ . \ / \ / \ / \ ? \ ? \ 46I- \ : \ / 0-6+(-+(03-9(7- \ : \ - 0))(E6(810(031(1+148>(0.9,0))(1$$

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 E_2 = +e (| \rangle \frac{(}{\sqrt{!}} \left(| \# \rangle | " \rangle | ! \rangle \right) (\\
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$$|\psi(0)\rangle = -(2|1\rangle + |2\rangle + |3\rangle)($$

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"")(O77(?/409(65(03-9(J;190-6+(./77(564(J;-.LB(93640(/+92149)((/' \90-: /01(031(762190(1+148>(?699-A71(231+(/+(171.046+(-9(.6+5-+1,(06(/(,-90/+.1(65("% (.:)((A' E31([hi(+:(>17762(7-+1(65(96,-;:(/4-919(546:(/+(1I.-01,(90/01(2-03(/(7-510-:1(564(6?0-./7(1:-99-6+(65("% (91.6+,9)((\90-:/01(031(+/0;4/7(2-,03(65(031(7-+1)((.' = 7;701((((, '(S-+, (031(1-81+=/7; 19(65(()(((-+(014:9(65(9;A9?/.19)((1'(F 3/0(/41(031(?699-A71(=/7;19(65(031(060/7(/+8;7/4(:6:1+0;:(0(564(/(,C171.046+T(((*+(1/.3(03191(90/0198(1=/7;/01(("\$)(,-41.0-6+B(1I?41991,(A>(/(=1.064(?601+0-/7((

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$$\begin{aligned} \hbar^{*} &= -\left(\frac{eB}{m}\right) S_{x}(x) \\ &(\\ O99; : 1031(++0-7/09/01(-9)() = \#^{**} = "!)^{*} = | + ! \rangle)(x) \\ &(\\ /'(_{-}/7, ; 7/01() = !)^{*} (x) \\ &(\\ /'(_{-}/7, ; 7/01() = !)^{*} (x) \\ &(\\ .'(_{-}/7, ; 7/01() (31(0 + :10, 121 +, 1+0)(+ .140)/+0)(+ ! + !)((_{-''_{2}})^{*} = \left<\frac{B_{1}}{2}\right> \left<\frac{B_{1}}{2}\right> (x) \\ &(\\ (x) \\ &= h \\ (x) \\ &= h \\ (x) \\ &(\\ (x) \\ &= h \\ (x) \\ &(\\ (x) \\ &= h \\ (x) \\ &(\\ (x) \\ &= h \\ (x) \\ &(\\ (x) \\ &= h \\ (x) \\ &(\\ (x)$$

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	/' _6:?;01(031(1+148>(.6441.0-6+(564(031(9>901:(-+(5-490(64,14(?140;4A/0-6+(03164>)(
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&%)($ \begin{array}{l} _6+9-, 14(/(6+10,-:1+9-6+/7(9J;/41(2177(?601+0-/7(65(2-,03(a(/+,(,1?03())(F1(-+01+,(06(90;,)<031(?46?140-19(65(031(A6;+,(90/01(65(/(?/4071(-+(03-9(2177(231+(-09(2-,03()(217(231+(-09(2-,03()(217(231+(-09(2-,03()(217(231+(-09(2-,03()(217(231+(-09(2-,03()(217(231+(-09(2-,03()(217(231+(-09(2-,03()(217(231+(-09(2-,03))))))$
(/'((M362(03/0(03141(-+,11,(1I-909(6+7>(6+1(A6;+,(90/01(/+,(./7.;7/01(-09(1+148>))(31.L(03/0(_(=/4-19(2-03(031(9J;/41(65(031(/41/(_(65(031(2177)(
(A'((W62(./+(031(?41.1,-+8(.6+9-,14/0-6+9(A1(/??7-1,(06(/(?/4071(?7/.1,(-+(031(?601+0-/7))(
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($!A'((\90/A7-93(031(419;70(03/0(A10211+(/+>(026(9;199-=1(+6,19(65(/(6+10),-:1+9-6+/7(A6;+,(90/01(2/=1(5;+.0-6+(,)*160(31(2/=1(5;+.0-6+(,)*1(65(/(3-8314(1+148>(90/018(,)*1(,,8(2-77(3/=1(/(71/90(6+1(+6,1)(1+148)))))))))))))))))))))))))))))))))))$

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